

## Section 1.5

What was done in 2 and 3 dimensions is extended to  $n$  dimensions

Matrix multiplication is introduced.

On page 60 the book is not clear what  $\mathbb{R}^n$  is. They call it Euclidean space.

Definitions:

Standard basis

Dot product = inner product

Length = norm of a vector

Use  $\|x\|^2 = x \cdot x$  in exercise 2a

Straightforward results in Theorem 3.

Theorem 4 (Cauchy-Schwarz inequality)

$$|x \cdot y| \leq \|x\| \|y\|$$

Theorem 5 (Triangle inequality)

$$\|x + y\| \leq \|x\| + \|y\|$$

## What we learn about matrices:

Matrix addition

Multiplying a matrix by a scalar

Matrix multiplication ← look in book

Identity matrix  $I_n$

Inverse of a matrix

Determinant of a matrix

## Properties:

$$I_n A = A I_n$$

$$(AB)C = A(BC)$$

$A(3B + 2C) = 3AB + 2AC$  and similar the other way round

## Theorem that is not proved:

If  $A$  is a square matrix then  $A$  is invertible if and only if  $\text{Det } A \neq 0$ .